

# Introduction to Robotics


Talk the Talk

## What is a robot?

"I can't define a robot, but I know one when I see one."  
-Joseph Engelberger

A robot is a machine built for real-world functions that is computer-controlled...  
...maybe.

Right: Room 8a microprocessor  
(from HowStuffWorks)



## Who's to say?

- Many devices with varying degrees of autonomy are called robots.
- Many different definitions for robots exist.
- Some consider machines wholly controlled by an operator to be robots.
- Others require a machine be easily reprogrammable.

## Japan?<sup>1</sup>

- *Manual-Handling Device*: controlled by operator
- *Fixed-Sequence Robot*: mechanical action sequence
- *Variable-Sequence Robot*: as 2 but modifiable
- *Playback Robot*: imitates human actions
- *Numerical Control Robot*: run by movement program
- *Intelligent Robot*: reactive to environment

1: Japanese Industrial Robot Association

## America and Europe?


- "a programmable, multifunction manipulator..."  
-RIA<sup>2</sup>
- "an independently acting and self controlling machine..."  
-ECM<sup>3</sup>

2: Robotics Institute of America  
3: European Common Market

## Robot Classes

- *Manipulators*: robotic arms. These are most commonly found in industrial settings.
- *Mobile Robots*: unmanned vehicles capable of locomotion.
- *Hybrid Robots*: mobile robots with manipulators.

(Images from AAAI and HowStuffWorks, respectively)



## Robot Components

- Body
- Effectors
- Actuators
- Sensors
- Controller
- Software

## Robot::Body

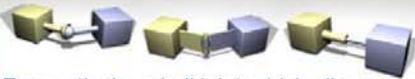
- Typically defined as a graph of *links* and *joints*:



A link is a part, a shape with physical properties.

A joint is a constraint on the spatial relations of two or more links.

## Types of Joints



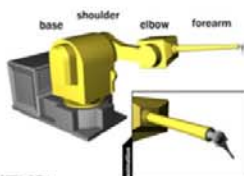
Respectively, a *ball joint*, which allows rotation around x, y, and z, a *hinge joint*, which allows rotation around z, and a *slider joint*, which allows translation along x.

These are just a few examples...

## Degrees of Freedom

- Joints constraint free movement, measured in "Degrees of Freedom" (DOFs).
- Links start with 6 DOFs, translations and rotations around three axes.
- Joints reduce the number of DOFs by constraining some translations or rotations.
- Robots classified by total number of DOFs

## 6-DOFs Robot Arm



How many DOFs can you identify in your arm?

## Robot::Effectors

- Component to accomplish some desired physical function
- Examples:
  - Hands
  - Torch
  - Wheels
  - Legs
  - Trumpet?



(Image from <http://www.toyota.co.jp/en/special/robot/>)

## Roomba Effectors

- What are the effectors of the Roomba?



## Roomba Effectors

- What are the effectors of the Roomba?



Vacuum, brushes, wheels

## Robot::Actuators

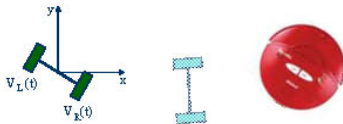
- Actuators are the “muscles” of the robot.
- These can be electric motors, hydraulic systems, pneumatic systems, or any other system that can apply forces to the system.

## Roomba Actuators

- The Roomba has five actuators, all electric motors:
  - Two drive wheels
  - One drives the vacuum
  - One drives the spinning side brush
  - One drives the agitator (spinning brush underneath)

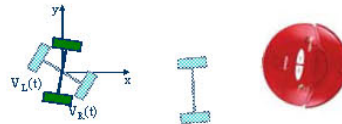
## Differential Steering

- The Roomba uses a differential steering system to turn and move forward. Each wheel is controlled by a distinct motor. Here, the Roomba rotates and moves forward.



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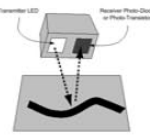
## Differential Steering!

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## Robot::Sensors

- Allow for perception.
- Sensors can be active or passive
- Active* – derive information from environment's reaction to robot's actions, e.g. bumpers and sonar.
- Passive* – observers only, e.g. cameras and microphones.



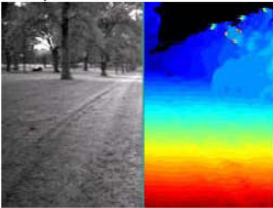
## Sensor Classes

- Range finders*: these sensors are used to determine distances from other objects, e.g. bumpers, sonar, lasers, whiskers, and GPS.



## Sensor Classes

- Imaging sensors*: these create a visual representation of the world.

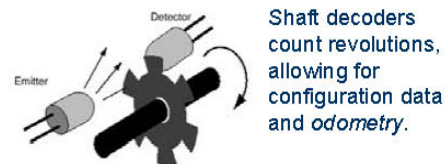


Here, a stereo vision system creates a depth map for a Grand Challenge competitor.

From NOVA, [www.pbs.org](http://www.pbs.org)

## Sensor Classes

- Proprioceptive sensors*: these provide information on the robot's internal state, e.g. the position of its joints.



Shaft decoders count revolutions, allowing for configuration data and *odometry*.

## Odometry

- Odometry is the estimation of distance and direction from a previously visited location using the number of revolutions made by the wheels of a vehicle.
- Odometry can be considered a form of "Dead Reckoning", a more general position estimation based on time, speed, and heading from a known position.

\*The Oxford English Dictionary does not recognize "deductive reasoning" as the basis of "dead reckoning"

## Odometry

- Odometry is good for short term, relative position estimation.
- However, uncertainty grows, shown by *error ellipses*, without bound.
- This is due to systematic and non-systematic errors.

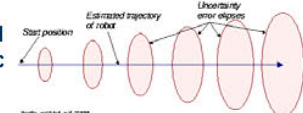


Figure 8.1: Growing "error ellipses" indicate the growing position uncertainty with odometry. (Adapted from [Tanouchi et al., 1994])

## Odometry, Non-systematic Errors

- These errors can rarely be measured and incorporated into the model.
- Error causes include uneven friction, wheel slippage, bumps, and uneven floors.

## Odometry, Systematic Errors

- Errors arising from general differences in model and robot behavior that can be measured and accounted for in the model, a process known as *calibration*.
- Two primary sources:
  - Unequal wheel diameters – lead to curved trajectory
  - Uncertainty about wheel base – lead to errors in turn angle

## Odometry, Position Updates

- With calibration, model behavior becomes more similar to observed behavior. However, estimation uncertainty still grows without bound.
- Position updates reduce uncertainty.



Figure 8.10: Different features can reduce the size of the robot's uncertainty ellipse in one or two directions. a, c. Walls and corners reduce uncertainty in one direction. b. Two adjacent walls at right angles reduce uncertainty in two directions. (Courtesy of [Bauer and Rosenau, 1995])

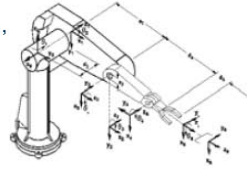
## Kinematics

- The calculation of position via odometry is an example of *kinematics*.
- Kinematics is the study of motion without regard for the forces that cause it.
- It refers to all time-based and geometrical properties of motion.
- It ignores concepts such as torque, force, mass, energy, and inertia.



## Forward Kinematics

- Given the starting configuration of the mechanism and joint angles, compute the new configuration.
- For a mechanism robot, this would mean calculating the position and orientation of the end effector given all the joint variables.



## Kinematics of Differential Steering

Derivation:

$$\frac{dx}{dt} = v(t) \cos(\theta(t)) \quad \text{X component of speed}$$

$$\frac{dx}{dt} = [(v_R - v_L) / 2] \cos(\theta(t)) \quad \text{Speed is average of } v_R \text{ \& } v_L$$

$$\frac{dy}{dt} = v(t) \sin(\theta(t)) \quad \text{Y component of speed}$$

$$\frac{dy}{dt} = [(v_R + v_L) / 2] \sin(\theta(t))$$

$$d\theta/dt = (v_R - v_L) / b \quad \text{Arc change over radius}$$

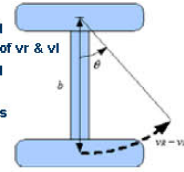
Integrate all:

$$\theta(t) = (v_R - v_L) t / b + \theta_0$$

$$x(t) = x_0 + \frac{b(v_R + v_L)}{2(v_R - v_L)} [\sin((v_R - v_L) t / b + \theta_0) - \sin(\theta_0)]$$

$$y(t) = y_0 + \frac{b(v_R - v_L)}{2(v_R + v_L)} [\cos((v_R - v_L) t / b + \theta_0) - \cos(\theta_0)]$$

This is the turn radius for a circular trajectory:  $(b/2)(v_R + v_L) / (v_R - v_L)$



## Kinematics of Differential Steering

- The above model has an asymptote when

$$v_R - v_L \approx 0$$

- When this occurs, special handling is required.

- Or a simpler model can be used:

$$\bar{v} = (s_R + s_L) / 2$$

$$\bar{\theta} = (s_R - s_L) / b + \theta_0$$

$$x = \bar{v} \cos(\bar{\theta}) + x_0$$

$$y = \bar{v} \sin(\bar{\theta}) + y_0$$

Here, SR and SL are measured right and left velocities. This approximates movement as a "point-and-shoot."

## Kinematics of Differential Steering

- Simpler approximations are often used when onboard computing power is lacking (or programmers are lazy!).
- However, the error grows quicker.
- A slightly better approximation:

$$\bar{v} = (s_R + s_L) / 2$$

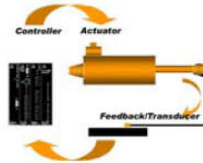
$$\bar{\theta} = (s_R - s_L) / 2b + \theta_0$$

$$x = \bar{v} \cos(\bar{\theta}) + x_0$$

$$y = \bar{v} \sin(\bar{\theta}) + y_0$$

## Robot::Controller

- Controllers direct a robot how to move.
- There are two controller paradigms
  - Open-loop controllers execute robot movement without feedback.
  - Closed-loop controllers execute robot movement and judge progress with sensors. They can thus compensate for errors.

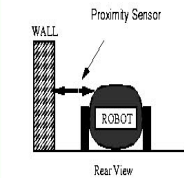


## Controller, Open-loop

- Goal: Drive parallel to the wall.
- Feedback: None.
- Result: Noisy movement, due to slippage, model inaccuracy, bumps, etcetera is likely to cause the robot to veer off the path.

Figure 11.1: Driving along a Wall Edge:

## Controller, Closed-loop



Using a Proximity Sensor to Measure Distance to a Wall

- Goal: walk parallel to the wall.
- Feedback: a proximity sensor
- Result: the robot will still veer away or toward the wall, but now it can compensate.

## Trajectory Error Compensation

- If a robot is attempting to follow a path, it will typically veer off eventually. Controllers design to correct this error typically come in three types:
  - *P controllers* provide force in negative proportion to measured error.
  - *PD controllers* are P controllers that also add force proportional to the first derivative of measured error.
  - *PID controllers* are PD controllers that also add force proportional to the integral of measured error.

## Roomba Control

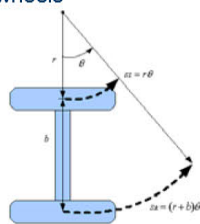
- The movement of the Roomba can be hard-coded ahead of time as an example of open-loop control.
- A path can be converted to Roomba wheel movement commands via *inverse kinematics*.

## Inverse Kinematics

- Inverse Kinematics is the reverse of Forward Kinematics. (!)
- It is the calculation of joint values given the positions, orientations, and geometries of mechanism's parts.
- It is useful for planning how to move a robot in a certain way.

## Kinematics<sup>-1</sup> of Differential Steering

- Vehicles using differential steering will go in a straight line if both wheels receive the same power.
- If both wheels turn at constant, but different, speeds, the vehicle follows a circular path
- Distances traveled:
  - $s_L = r \theta$
  - $s_R = (r + b) \theta$
  - $s_M = (r + b / 2) \theta$



## Kinematics<sup>-1</sup> of Differential Steering

- This calculation ignores acceleration, but it can be used to calculate how to move a device using a differential steering system, such as a Roomba, along a path that consists of lines and arcs.

